CSCI: 4500/6500 Programming Languages

Functional Programming Languages Part 3: Evaluation and Application Cycle Lazy Evaluation





Back to the Basics: Steps in

Inventing a Language

Design the grammar

- » What strings are in the language?
- » Use BNF to describe all the strings in the language

Make up the evaluation rules

» Describe what everything the grammar can produce means

Build an evaluator

- » A procedure that evaluates expressions in the language
 - The evaluator, which determines the meaning of expressions in the programming language, is just another program.

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Programming an Evaluator

 If a language is just a program, what *language* should we program the language (evaluator) in?

Metacircular Evaluator

 An evaluator that is written in the same language that it evaluates is said to be metacircular

Sounds like recursion: It's circular recursion. There is no termination condition. It's a chicken-and-the-egg kind of thing. (There's actually a hidden termination condition: the bootstrapping process.)

- One more requirement: The language interpreted does not need additional definitions of semantics other than that is defined for the evaluator (sounds circular).
 - » Example: The C compiler is written is C but not meta circular because the compiler specifies extremely detailed and precise semantics for each and every construct that it interprets.

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Evaluation Basics

To evaluate a combination:

- Evaluate each element (all the subexpressions) of the combination
- Apply the procedure to the value of the leftmost subexpression (the operator) to the arguments that are the values of the other subexpressions (the operands)

	alua nbir				is applied o	on 4
(*	(+	2	(*	4	6))	
	(+	3	5	7))	

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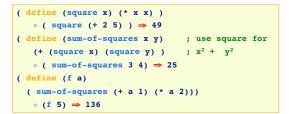
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Observation: This is recursive

Example: Procedural Building Blocks



- square is a compound procedure which is given the name square which is represents the operation of multiplying something by itself.
- Evaluating the definition creates the compound procedure and associates it with the name square (lookup)
- Application: To apply a compound procedure to arguments, evaluate the body of the procedure with each formal parameter replaced by the 'real' arguments. <u>unsubstitution model -- an assignment model <-variable<-env)</u>

Environmental Model of Evaluation

- 1. To evaluate a combination (compound expression)
 - evaluate all the subexpressions and then
 - apply the value of the operator subexpression (first expression) to the values of the operand subexpressions (other expressions).
- 2. To apply a procedure to a list of arguments,
 - evaluate the body of the procedure in a new environment (by a frame) that binds the formal parameters of the procedure to the arguments to which the procedure is applied to.



Core of the Evaluator

Basic cycle in which

- » expressions to be evaluated in environments are
- » reduced to procedures to be applied to arguments,
- Which in turn are reduced to new expressions
 - » to be evaluated in new environments, and so on,
 - » until we get down to

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- symbols, whose values are looked up in the environment
- primitive procedures, which are applied directly.



The evaluator - metacircularity (eval expression environment)

- Evaluates the the expression relative to the environment
 - » Examples: environments (returns a specifies for the environment) - scheme-report-environment version
 - null-environment version
- Primitives:
 - $\ensuremath{\, {\rm self}}$ evaluating expressions, such as numbers, $\ensuremath{\, {\rm eval}}$ returns the expression itself
 - » variables, looks up variables in the environment
- Some special forms (lambda, if, define etc). eval provide direct implementation:
 - » Example: quoted: returns expression that was quoted
- Others lists:

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» eval calls itself recursively on each element and then calls apply, passing as argument the value of the first element (which must be a function) and a list of the remaining elements. Finally, eval returns what apply returned at Moment, UAA

Eval

(define	(eval exp env)						
(cond	((self-evaluating? exp) exp)						
	((variable? exp) (lookup-variable-value exp env))						
	(quoted? exp) (text-of-quotation exp))						
	((assignment? exp) (eval-assignment exp env))						
	((definition? exp) (eval-definition exp env))						
	((if? exp) (eval-if exp env))						
	((lambda? exp)						
	(make-procedure (lambda-parameters exp)						
	(lambda-body exp)						
env))							
	((begin? exp)						
	(eval-sequence (begin-actions exp) env))						
	((cond? exp) (eval (cond->if exp) env))						
	((application? exp)						
	(apply (eval (operator exp) env)						
	<pre>(list-of-values (operands exp) env)))</pre>						
	(else						
	(error "Unknown expression type - EVAL" exp)))						

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Eval: Example

- (eval '(* 7 3) (scheme-report-environment 5)) => 21
- (eval (cons '* (list 7 3)) (scheme-report-environment 5)) => 21

Current Scheme doesn't recognize `scheme-report-environment'

apply

Apply

are)

- apply applies its first argument (a function) and applies it to its second argument (a list) => 9
- (apply max '(3 7 2 9)) • Primitive function, apply invokes it.
- Non-primitive function (f),
 - Retrieves the referencing environment in which the function's lambda expression was originally evaluated and adds the names of the function's parameters (the list) (call this resulting environment (e))
 - » Retrieves the list of expressions that make up the body of f. » Passes the body's expression together with e one at a time to eval. Finally, apply returns what the eval of the last expression in the body of f returned.

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```
(cond ((primitive-procedure? proce
 (apply-primitive-procedure procedure arguments))
((compound-procedure? procedure)
 (eval-sequence
  (procedure-body procedure)
   (extend-enviro
    (procedure-parameters procedure)
     arguments
    (procedure-environment procedure))))
(else
(error
  "Unknown procedure type - APPLY" procedure))))
```

(define (apply procedure arguments)

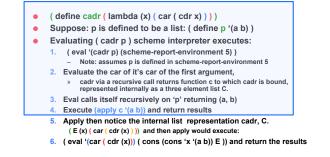
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Example: Evaluating (cadr p)

- (define cadr (lambda (x) (car (cdr x))))
- Stored Internally as three element list C: (E (x) (car (cdr (x)))) surrounding referencing environment (global)
 - list of parameters (x)
 - list of body expressions (one element: (car (cdr x)))
 - Suppose: p is defined to be a list: (define p '(a b))
- (cadr p) => b
- Evaluating (cadr p) scheme interpreter executes: » (eval '(cadr p) (scheme-report-environment 5))
 - Note: assumes p is defined in scheme-report-environment 5
 - 1. Evaluate the car of it's car of the first argument,
 - » cadr via a recursive call returns function c to which cadr is bound, represented internally as a three element list C.
 - 2. Eval calls itself recursively on 'p' returning (a, b) 3. Execute (apply c '(a b)) and return results
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Example: Evaluating (cadr p)



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Summary of Scheme

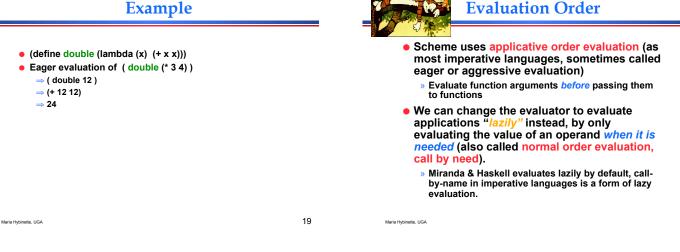
- The core of a Scheme evaluator is eval and apply, procedures that are defined in terms of each other.
 - » The eval procedure takes an expression and an environment and evaluates to the value of the expression in the environment;
 - » The apply procedure takes a procedure and its operands and evaluates to the value of applying the procedure to its operands.

Evaluation Order

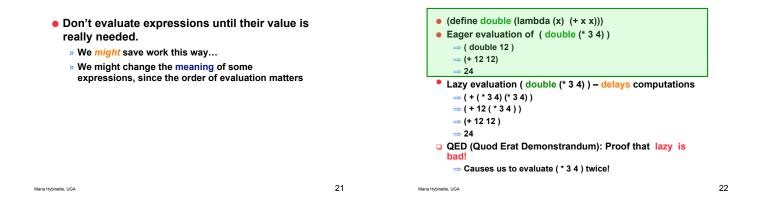
- Scheme uses applicative order evaluation (as most imperative languages, sometimes called eager or aggressive evaluation)
 - Evaluate function arguments before passing them to functions

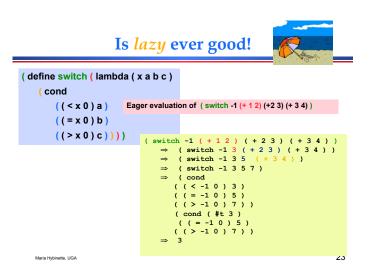


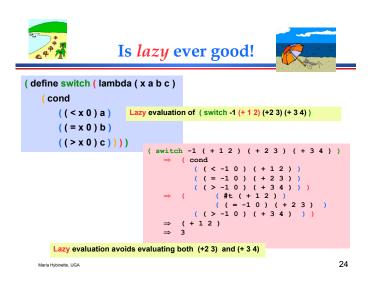
Example



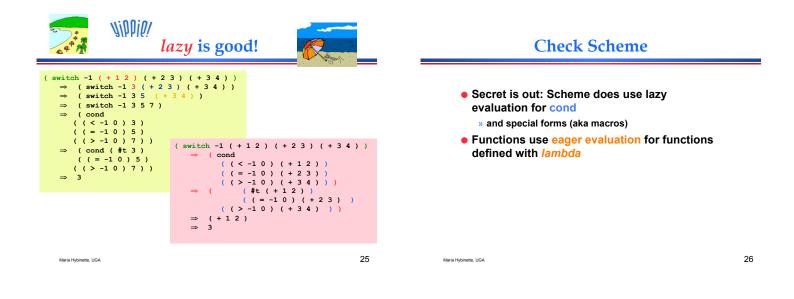
Lazy Evaluation

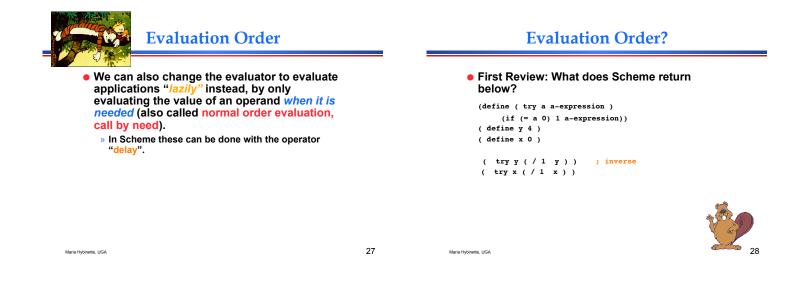






Check: Is being Lazy any Good?





Evaluation of Argument Summary

- Applicative Order ("eager evaluation") » Evaluate all subexpressions before apply
 - » The standard Scheme rule, Java
- Normal Order ("lazy evaluation")
 - » Evaluate arguments just before the value is needed
 - » Algol60 (sort of), Haskell, Miranda

"Normal" Scheme order is not "Normal Order"!

(define double (lambda (x) (+ x x)))

try with 2 arguments

(define y 4) (define x 0)

(define (try a a-expression) ; (try a (a-expression)) => evaluates (if (= a 0) 1 a-expression)) ; inner expression first : problem if a = 0 even with if test.

; (try y (/ 1 y)) ; (try x (/ 1 x))

; impact evaluation order by using lazy evaluation 'delay' in scheme (define (delay-inverse x) (delay (/ 1 x))) ; (try x (delay-inverse 0)) (define (aggressive-inverse x) (/ 1 x)) ; (try x (aggressive-inverse 0))

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Strict and Non-Strict Languages

- A strict language requires all arguments to be well-defined, so applicative (eager) order can be used
- A non-strict language does not require all arguments to be well-defined; it requires normal-order (lazy) evaluation

Comparing Functional and Imperative Languages

- Imperative Languages:
 - » Efficient execution
 - » Complex semantics
 - » Complex syntax
 - » Concurrency is programmer designed
- Functional Languages:
 - » Simple semantics
 - » Simple syntax
 - » Inefficient execution
 - » Programs can automatically be made concurrent

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Functional Programming in Perspective (pros)

Advantages of functional languages

- » lack of side effects makes programs easier to understand
- » lack of explicit evaluation order (in some languages) offers possibility of parallel evaluation (e.g. MultiLisp)
- » lack of side effects and explicit evaluation order simplifies some things for a compiler (provided you don't blow it in other ways)
- » programs are often surprisingly short
- » language can be extremely small and yet powerful

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Functional Programming in Perspective (cons)

Advantages of functional languages

» difficult (but not impossible!) to implement efficiently on von Neumann machines

- lots of copying of data through parameters
- (apparent) need to create a whole new array in order to change one element
- heavy use of pointers (space/time and locality problem)
- frequent procedure calls
- heavy space use for recursion
- requires garbage collection
- requires a different mode of thinking by the programmer
- difficult to integrate I/O into purely functional model

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