

# CSCI: 4500/6500 Programming Languages

## Control Flow Chapter 6



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# Big Picture: Control Flow Ordering in Program Execution

## Ordering/Flow Mechanisms:

- **Sequencing** (statements executed (evaluated) in a specified order)
  - Imperative language - very important
  - Functional - doesn't matter as much (emphasizes evaluation of expression, de-emphasize or eliminates statements, e.g., pure fl don't have assignment statements)
- **Selection** -- Choice among two or more
  - De-emphasized in logical languages
- **Iteration**
  - » Repeating structure
    - emphasized in imperative languages
- **Procedural abstraction, recursion**, requires stack
- **Concurrency**
  - » 2 or more code fragments executed at the same time
- **Non-determinacy** (unspecified order)

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# Expression Evaluation: Classification Outline

- Infix, Prefix or Postfix
- Precedence & Associativity
- Side effects
- **Statement** versus **Expression** Oriented Languages
- Value and Reference Model for Variables
- Orthogonality
- Initialization
- Aggregates
- Assignment

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# Evaluation: \* fix operators

- **Expression:**
  - » **Operator** (built-in function) and **operands** (arguments)
- **Infix, prefix, postfix operators**
  - » (+ 5 5) or 5 + 6
  - » operators in many languages are just `syntactic sugar'<sup>1</sup> for a function call:
    - $a + b \Rightarrow a.operator+(b)$  in C++
    - “\*(a, b) in Ada
  - » Cambridge Polish prefix and function name *inside* parenthesis.
  - » Postfix - postscript, Forth input languages, calculators

<sup>1</sup> Landin "adding "sugar" to a language to make it easier to read (for humans)

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# Expression Evaluation: Precedence & Associativity

How should this be evaluated?

- $a + b * c ** d ** e / f$

How about?

- $((((a + b) * c) ** d) ** e) / f$
- $a + (((b * c) ** d) ** (e / f))$
- $a + ((b * (c ** (d ** e))) / f)$ 
  - » Fortran does this last option
- **or something else?**

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# Precedence & Associativity

- **Precedence** specify that some operators group more tightly and others
  - » Richness of rules across languages varies (overview next slide)
- **Associativity** rules specify that sequences of operators of *equal* precedence groups either left or right (or up or down? for a weird language of your own creation)
  - » Associativity rules are somewhat uniform across languages but there are variations

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Fortran	Pascal	C	Ada
**	not	** , - (post-inc., dec.)	abs (absolute value), not, **
*, /	*, /, div, mod, and	* (binary), /, % (modulo/division)	*, /, mod, rem
*, - (unary and binary)	*, - (unary and binary), or	*, - (binary)	*, - (unary)
.eq., .ne., .lt., .le., .gt., .ge. (comparisons)	<, <=, >, >=, =, <>, III	<, <=, >, >= (inequality tests)	==, /=, <, <=, >, >=
.not.	..=, != (equality tests)	==, != (equality tests)	
	& (bit-wise and)	& (bit-wise and)	
	^ (bit-wise exclusive or)	^ (bit-wise exclusive or)	
	(bit-wise inclusive or)	(bit-wise inclusive or)	
.and.	&& (logical and)	&& (logical and)	and, or, xor (logical operators)
.or.	(logical or)	(logical or)	
.eqv., .neqv. (logical comparisons)	?: (if...then...else)	?: (if...then...else)	
	=, +=, -=, **, /%, >>=, <<=, &=, ^=,  = (assignment)	=, +=, -=, **, /%, >>=, <<=, &=, ^=,  = (assignment)	
	, (sequencing)	, (sequencing)	

Figure 6.1: Operator precedence levels in Fortran, Pascal, and C. Operators at the top of the figure group most tightly.

**Example Precedence:**

- if A < B and C < D then K = 5
- How would Pascal evaluate this?
- A < (B and C) < D

## Precedence

- Most languages avoid this problem by giving arithmetic operators higher precedence than relational (comparison) operators.

## Precedence: Rule of Thumb

- C has 15 levels - **too many** to remember
- Pascal has 3 levels - **too few** for good semantics
- Fortran has 8
- Ada has 6
  - » Note: Ada puts **and, or** at same level
- **Lesson:** when unsure (e.g., programmer using many languages, better to circumvent precedence and use parentheses!

## Associativity Example

- Basic operators almost always **left to right**
  - » 9-3-2 = (9-3)-2 = 4 (left right) →
  - » 9-3-2 = 9-(3-2) = 8 (right-left) ←
- Exponential operator: \*\*
  - » **right-left** (as do mathematics) in Fortran
    - 4\*\*3\*\*2 = 4\*\*(3\*\*2) = 262,144
  - » Language syntax **requires** parenthesized form (Ada)
- Assignment '=' in expressions associates: **right-left** ←
  - » a = b = a + c => a = ( b = (a+c) )
    - assigns (a+c) to b then assigns the same value to a

## Side Effects & Idempotent Functions

**Side Effects** – a function has a **side effect** if it **influences subsequent computation** in any way other than by **returning a value**. A side effect occurs when a function **changes the environment** in which it exists

**Idempotent** – an idempotent function is one that if called again with the same parameters, will always give the same result

**Referentially transparent** - Expressions in a purely functional language are referentially transparent, their value depends only on the referencing environment.

**Imperative programming** – “Programming with side effects” (programming in terms of statements, state).

## Side Effects

- **Assignment statements** provide the ultimate example of side effects
  - they change the value of a variable
  - Fundamental in the von Neumann model of computation.
- Several languages *outlaw side effects* for functions (these languages are called *single assignment* languages)
  - » easier to prove things about programs
  - » closer to Mathematical intuition
  - » easier to optimize
  - » (often) easier to understand
- **But side effects can be nice: consider - rand()**
  - Needs to have a side effect, or else the same random number every time it is called.

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## Side Effects (cont)

- Side effects are a particular problem if they affect **state used in other parts** of the expression in which a function call appears:
- **Example:**
  - » `a - f(b) - c * d /* f(b) may affect 'd' */`
  - » **What is evaluated first:**
    - `a - f(b)`
    - `c * d`

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## Ordering within Expressions

- **Another Example:**
  - » `f(a, g(b), c)` which parameter is evaluated first?
- **Why is it important:**
  - » **Side-effects:**
    - if `g(b)` modifies `a` or `c` then the values passed into `f` will depend on the order that parameters are evaluated
  - » **Code improvements:**
    - `a = B[i]`
    - `c = a * b + d * 3`
      - Note: precedence or associativity does not say if we evaluated `a*b` or `d*3` first.
    - Evaluate: `d*3` first, so the previous load (slow) of `B[i]` from memory occurs in parallel of a doing something different, i.e. computing `d*3`.

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## Evaluation of Operands and Side Effects

```
int x = 0;

int foo()
{
  x += 5;
  return x;
}

int a = foo() + x + foo();

What is the value of a?
a = 5 + x + foo()
```

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## Re-ordering using mathematical properties

- **Commutative**
  - »  $(a+b) = (b+a)$
- **Associative**
  - »  $(a+b) + c = a + (b + c)$
- **Distributive**
  - »  $a * (b + c) = a * b + a * c.$

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## Mathematical Identities

**Example:**

```
a = b + c
d = c + e + b
```

**Re-order to:**

```
a = b + c
d = b + c + e (already evaluated b+c (it is a))
```

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## Mathematical Identities

- **Problem: Computer has limited precision**
  - » associativity (known to be dangerous)
    - $(a + b) + c$
    - works if  $a \neq \text{maxint}$  and  $b \neq \text{minint}$  and  $c < 0$
    - $a + (b + c)$  does not

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## Expression vs. Statement Orientation

- **Statements :**
  - » executed solely for their side effects and
  - » return no useful value
  - » most imperative languages
  - » time dependent
- **Expressions :**
  - » may or may not have side effects
  - » always produces a value and
  - » functional languages (Lisp, Scheme, ML)
  - » time less
- **C kinda halfway in-between (distinguishes)**
  - » allows expression to appear instead of statement

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## Assignment

- **statement (or expression) executed for its side effect**
- **assignment operators (+=, -=, etc)**
  - » handy
  - » avoid redundant work (or need for optimization)
    - No need for redundant address calculations (guaranteed)
  - » perform side effects exactly once (avoids peculiarities)
    - $A[f(i)] = A[f(i)] + 1$  ( $f(i)$  may have a side effect  $\times 2$ ).
    - $A[f(i)] += 1$

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## References and Values

- **Assignment seems straightforward**
- **Semantic differences depending if languages uses a**
  - » **A reference model**
  - » or **value model** of variables.
- **Impact on programs that use pointers (we will talk more about pointers after Spring break).**

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## Value Model

a 4

- **Variable is a named container for a value**
- **left-hand side of expressions denote "locations" and are referenced as l-values**
- **right-hand side of expressions denote "values" and are referred to as r-values**
- **Expressions can be either an l-value or an r-value depending on context:**
  - »  $2 + 3 = a$
  - »  $a = 2 + 3$
  - »  $(f(x)+3) \rightarrow b[c] = 2$  /\* l-value expression \*/
  - »  $k = (f(x)+3) \rightarrow b[c]$

Example languages who use value model: C and C++

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## Value Model: Example

a 4

a 4  
b 2  
c 2

b = 2  
c = b  
a = b + c

1. Put the value 2 in b
2. Copy value of b into c
3. Read b and c and put result in a

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## Reference Model

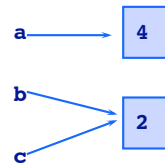


- **Variable is a named reference to a value**
- **Every “value” is a l-value (location)**
  - » Only one '4', variables points to the '4', Above the variable **a** points to '4'
- **To get a “value” (r-value) need to dereference it to obtain value that it contain (points to).**
  - » Most languages this dereferencing is automatic, e.g., Clue. In ML need to explicit dereference it.
  - » Indirection for accesses (however most compiler use multiple copies of objects to speed things up).

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## Reference Model

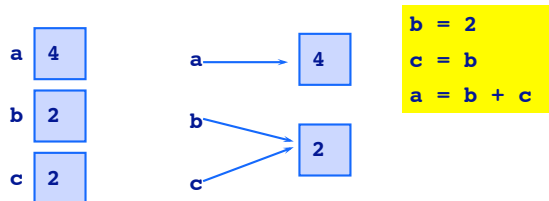


```
b = 2
c = b
a = b + c
```

1. Let b refer to 2
2. Let c also refer to 2
3. Pass these references to '+'
4. Let a refer to the result, namely 4

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- **Value model:** any integer value can contain the value 2
- **Reference model:** only one 2 (if variable on right side, need to dereference to get actual value).

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## Value/Variable Model Implications

- **Reference model need to distinguish between variables that**
  - » refer to the same object and variables that
  - » point to different objects but that have the same “value” (happens to be equal)
- **LISP provided two notions of equality to distinguish between the two.**

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## Value versus Reference Models

- **Value-oriented languages**
  - » C, Pascal, Ada
- **Reference-oriented languages**
  - » most functional languages (Lisp, Scheme, ML)
  - » Clu, Smalltalk
- **Algol-68 kinda halfway in-between**
- **Java deliberately in-between, uses both:**
  - » Value model for built-in types (int, double)
  - » Reference model for user-defined types (**objects**)
- **C# and Eiffel allow programmer choose model for user defined types.**

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## Orthogonality

- **Features that can be used in any combination (no redundancy)**
  - » Meaning makes sense
  - » Meaning is consistent

```
if (if b != 0 then a/b == c else false) then ...
if (if f then true else messy()) then ...
```
- **Algol makes orthogonality a principal design goal.**

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## Initialization

### Motivation:

- Improve execution time: Statically allocated variables (by compiler)
  - » e.g. reduce cost of assignment statement at run time.
- Avoid (weird) errors of evaluating variables with no initial value

### Approach:

- Pascal has no initialization facility (assign)
- C/C++ initializes static variables to 0 by default
- Usage of non-initialized variables may cause a hardware interrupt (implemented by "initializing" value to NaN)
- Constructor: automatic initialization at run-time

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## Control Flow

(Really)



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## Structured vs. Unstructured Control Flow

**Structured Programming** – hot programming trend in the 1970's

- Top down design
- Modularization of code
- Structured types
- Descriptive variable names
- Extensive commenting
- After Algol 60, most languages had: if...then...else, while loops

Don't need to use **goto's** ...

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## Types of Control Flow

- **Sequencing** -- statements executed (evaluated) in a specified order
  - » Imperative language - very important
  - » Functional - doesn't matter as much (emphasizes evaluation of expression, de emphasize or eliminates statements, e.g. assignment statements)
- **Selection** -- Choice among two or more
  - Deemphasized in logical languages
- **Iteration** -- Repeating structure
  - emphasized in imperative languages
- **Procedural abstraction**
- **Recursion**, requires stack
- **Concurrency** executing statements at the same time
- **Non-determinacy** -- unspecified order

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## Sequencing

- **Simple idea**
  - » Statements executes one after another
  - » Very imperative, von-Neuman
  - » Controls order in which side effects occur
- **Statement blocks**
  - » groups multiple statement together into one statement
  - » Examples:
    - {} in C, C++ and Java
    - begin/end in Algol, Pascal and Modula
- **Basic block**
  - » Block where the only control flow allowed is sequencing

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## Selection



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## if statements

- **if condition then statement else statement**
  - » Nested if statements have a dangling else problem

## Dangling else Problem

```
if ... then
    if ... then
        else ...
```

- **OR**

```
if ... then
    if then ...
else ...
```
- Which one does the else map to?

## Dangling else Problem

- **ALGOL:**
  - » does not allow “then if”
  - » statement has to be different than another **if** statement (can be another block, that contains an **if**)
- **Pascal:**
  - » **else** associates with closest unmatched **then**
- **Perl:**
  - » Has a separate **elsif** keyword (in addition to **else** and **if**)
  - » “**else if**” will cause an error

## Strict vs short-circuit evaluation of conditions

- **strict**
  - » Evaluate **all** operands before applying operators
    - Pascal
- **short-circuit**
  - » Skip operand evaluation when possible
  - » Evaluation order important
    - if operand-evaluation has side effects (seen)
    - if programmer knows that some operands can be computed more quickly than others
  - » Examples
    - **||** and **&&** in C++ and Java
      - always use short-circuit evaluation
    - **then if and or else** in Ada
      - language supports both strict and short-circuit, programmer decides: use **and**, **or** for strict evaluation

## Short Circuiting

- **C++**

```
p = my_list;
while( p && p->key != val )
    p = p->next;
```
- **Pascal**

```
p := my_list;
while( p <> nil) and ( p^.key <> val ) do
    p := p^.next
```

Ouch!

## Short Circuit Jump Code

```
if ((A > B) and (C > D)) or (E <> F) then
    then_clause
else
    else_clause
```

- Usually purpose of condition is to *create a branch instruction* to various locations not a value to be stored.

## No Short Circuiting (Pascal)

```

r1 := A      -- load
r2 := B
r1 := r1 > r2
r2 := C
r3 := D
r2 := r2 > r3
r1 := r1 & r2
r2 := E
r3 := F
r2 := r2 $<>$ r3
r1 := r1 $|$ r2
if r1 = 0 goto L2
L1: then_clause -- label not actually used
    goto L3
L2: else_clause
L3:
    
```

```

if ((A > B) and (C > D)) or (E <> F) then
    then_clause
else
    else_clause
    
```

- root would name r1 as the register containing the expression value

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## Short Circuiting

```

r1 := A
r2 := B
if r1 <= r2 goto L4
r1 := C
r2 := D
if r1 > r2 goto L1
L4: r1 := E
    r2 := F
    if r1 = r2 goto L2
L1: then_clause
    goto L3
L2: else_clause
L3:
    
```

```

if ((A > B) and (C > D)) or (E <> F) then
    then_clause
else
    else_clause
    
```

- Inherited attributes of the conditions root would indicate that control should “fall through” to L1 if the condition is true, or branch to L2 if false.
- Value of ‘final’ expression never in a register rather its value is implicit in the control flow.

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## Implications

- Short-circuiting
  - » Can avoid out of bound errors
  - » Can lead to more efficient code
  - » Not all code is guaranteed to be evaluated
- Strict
  - » Not good when code has build in side effects

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## Case/Switch Statements

- Alternative to nested if...then...else blocks

```

j := ... (* potentially complicated expression *)
IF j = 1 THEN clause_A
ELSEIF j IN 2,7 THEN clause_B
ELSEIF j IN 3..5 THEN clause_C
ELSEIF (j = 10) THEN clause_D
ELSE clause_E
END
CASE ... (* potentially complicated expression *) of
    1:      clause_A
    | 2, 7: clause B
    | 3..5: clause C
    | 10:   clause D
    ELSE   clause E
END
    
```

Principal motivation of case statement is to generate efficient target code not syntactic elegance.

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## Implementation of Case Statements

- If...then...else

```

r1 := ...
if r1 <> 1 goto L1
clause_A
goto L6
L1: if r1 = 2 goto L2
    if r1 <> 7 goto L3
L2: clause_B
    goto L6
L3: if r1 < 3 goto L4
    if r1 > 5 goto L4
    clause_C
    goto L6
L4: if r1 <> 10 goto L5
    clause_D
    goto L6
L5: clause_E
L6:
    
```

- Case (uses jump table)

```

T: &L1      -- tested expression = 1
   &L2
   &L3
   &L3
   &L3
   &L5
   &L2
   &L5
   &L5
   &L4
L6: r1 := ... -- tested expression = 10
    if r1 < 1 goto L5
    if r1 > 10 goto L5 -- L5 is the "else" arm
    r1 := 1
    r2 := T[r1]
    goto *r2
L7:
    
```

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## Case vs Switch

- Switch is in C, C++, and Java
  - » Unique syntax
  - » Use **break** statements, otherwise statements fall through to the next case
- Case is used in most other languages
  - » Can have ranges and lists
  - » Some languages do not have **default** clauses
    - Pascal

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## Origin of Case Statements

- Descended from the computed **goto** of Fortran

```
goto (15, 100, 150, 200), J
```

```
if J is 1, then it jumps to label 15
if J is 4, then it jumps to label 200
if J is not 1, 2, 3, or 4, then the
statement does nothing
```

## Iteration



## Iteration

- More prevalent in imperative languages
- Takes the form of loops
  - » Iteration of loops used for their side effects
    - Modification of variables

## Iteration

### Two (2) kinds of iterative loops:

- **enumeration controlled:** Executed once for every value in a given finite set (iterations known before iteration begins)
- **logically-controlled:** Executed until some condition changes value

## Enumeration-Controlled Loop

- Early Fortran:

```
do 10 i = 1, 50, 2
. . .
10: continue
```
- Equivalent?

```
10: i = 1
. . .
i = i + 2
if i <= 50 goto 10
```

## Issue #1

- Can the step size/bounds be:
  - » Positive/negative ?
  - » An expression ?
  - » Of type Real ?

## Issue #2

- Changes to loop indices or bounds
  - » Prohibited to varying degrees
  - » Algol 68, Pascal, Ada, Fortran 77/90
    - Prohibit changes to the index within loop
    - Evaluate bound once (1) before iteration

## Changes to loop indices or bounds

- A statement is said to **threaten** an index variable if
  - » Assigns to it
  - » Passes it to a subroutine
  - » Reads it from a file
  - » Is a structure that contains a statement that threatens it

## Issue #3

- Test terminating condition before first iteration
- Example:

```
for i := first to last by step do
```

```
...
```

```
end
```

```
r1 := first
r2 := step
r3 := last
L1: if r1 > r3 goto L2
...
r1 := r1 + r2
goto L1
L2
```

```
r1 := first
r2 := step
r3 := last
L1: ...
r1 := r1 + r2
goto L1
L2: if r1 < r3 goto L1
```

## Issue #4

- Access to index outside loop
  - » undefined
    - Fortran IV, Pascal
  - » most recent value
    - Fortran 77, Algol 60
  - » index is a local variable of loop
    - Algol 68, Ada

## Issue #5

- Jumps
  - » Restrictions on entering loop from outside
    - Algol 60 and Fortran 77 and most of their descendants prevent the use of gotos to jump into a loop.
  - » “exit” or “continue” used for loop escape

## Summary Issues

- step: size (pos/neg), expression, type
- changes to indices or bounds within loop
- test termination condition before first iteration of loop
- scope of control variable (access outside loop)
  - » value of index after the loop

## Logically Controlled Loops

```
while condition do statement
```

- Advantages of for loop over while loop

- » Compactness
- » Clarity
- » All code affecting flow control is localized in header

## Logically Controlled Loops

- Where to test termination condition?

- » pre-test (while)
- » post-test (repeat)
- » mid-test (when)
  - one-and-a-half loops (loop with exit, mid-test)

```
loop:
  statement list
when condition exit
  statement list
when condition exit
end loop
```

## C's for loop

- C's for loop

- » Logically controlled
  - Any enumeration-controlled loop can be written as a logically-controlled loop

```
for( i = first; i <= last; I += step )
{
}
```

```
i = first;
while( i <= last )
{
  i += step;
}
```

## C's for loop

- Places additional responsibility on the programmer

- » Effect of overflow on testing of termination condition
- » Index and variable in termination condition can be changed
  - By body of loop
  - By subroutines the loop calls

## Combination Loops

- Combination of enumeration and logically controlled loops
- Algol 60's for loop

*For\_stmt* -> *for id := for\_list do stmt*

*For\_list* -> *enumerator (, enumerator)\**

*Enumerator* -> *expr*

-> *expr step expr until expr*

-> *expr while condition*

## Algol 60's for loop

- Examples: (all equivalent)

```
for i := 1, 3, 7, 9 do...
```

```
for i := 1 step 2 until 10 do ...
```

```
for i := 1, i + 2 while i < 10 do ...
```

- Problems

- » Repeated evaluation of bounds
- » Hard to understand

## Iterators: HW - Read in Textbook

- True Iterators
- Iterator Objects
- Iterating with first-class functions
- Iterating without iterators

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## Recursion



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## Recursive Computation

- Decompose problem into smaller problems by calling itself
- **Base case**- when the function does not call itself any longer; no base case, no return value
- Problem must always get smaller and approach the base case

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## Recursive Computation

- No side effects
- Requires no special syntax
- Can be implemented in most programming languages; need to permit functions to call themselves or other functions that call them in return.
- Some languages don't permit recursion: Fortran 77

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## Tracing a Recursive Function

```
(define sum (lambda(n)
  (if (= n 0)
      0
      (+ n (sum (- n 1))))))
```

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## Tracing a Recursive Function

```
>(trace sum)
#<unspecified> >
>(sum 5)
"CALLED" sum 5
"CALLED" sum 4
"CALLED" sum 3
"CALLED" sum 2
"CALLED" sum 1
"CALLED" sum 0
"RETURNED" sum 0
"RETURNED" sum 1
"RETURNED" sum 3
"RETURNED" sum 6
"RETURNED" sum 10
"RETURNED" sum 15
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```

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A screenshot of the DrScheme IDE. The left pane shows the definition of a recursive sum function: 

```
(define sum (lambda (n)
  (if (= n 0)
      0
      (+ n (sum (- n 1))))))
```

The right pane shows the output of the function, including a welcome message and a detailed trace of the recursive calls and returns. The trace shows the function being called with arguments 5, 4, 3, 2, 1, and 0, and returning values 0, 1, 3, 6, 10, and 15 respectively.

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## Embedded vs. Tail Recursion

**Analogy:** You've been asked to measure the distance between UGA and Georgia Tech

**Embedded:**

1. Check to see if you're there yet
2. If not, take a step, put a mark on a piece of paper to keep count, restart the problem
3. When you're there, count up all the marks

**Tail:**

1. Write down how many steps you're taken so far as a running total
2. When you get to Georgia Tech, the answer is already there; no counting!

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## Recursion

- **Tail recursion:** No computation follows recursive call

```
/* assume a, b > 0 */
int gcd (int a, int b)
{
    if (a == b) return a;
    else if (a > b) return gcd (a - b, b);
    else return gcd (a, b - a);
}
```

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## Which is Better?

- **Tail.**
- Additional computation never follows a recursive call; the return value is simply whatever the recursive call returns
- The compiler can reuse space belonging to the current iteration when it makes the recursive call
- Dynamically allocated stack space is unnecessary

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- Any logically controlled iterative algorithm can be rewritten as a recursive algorithm and vice versa
- **Iteration:** repeated modification of variables (imperative languages)
  - » Uses a repetition structure (for, while)
  - » Terminates when loop continuation condition fails
- **Recursion:** does not change variables (functional languages)
  - » Uses a selection structure (if, if/else, or switch/case)
  - » Terminates when a base case is recognized

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## Tail Recursion Example

```
/* assume a, b > 0 */
int gcd (int a, int b)
{
    if (a == b) return a;
    else if (a > b) return gcd (a -
    b, b);
    else return gcd (a, b - a);
}
```

```
/* assume a, b > 0 */
int gcd (int a, int b)
{
    start:
        if ( a == b ) return a;
        else if ( a > b )
            {
                a = a - b;
                goto start;
            }
        else
            {
                b = b - a;
                goto start;
            }
}
```

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## Which is tail recursive?

```
(define summation (lambda (f low high)
  (if (= low high)
      (f low)
      (+ (f low) (summation f (+ low 1) high))))))

(define summation (lambda (f low high subtotal)
  (if (= low high)
      (+ subtotal (f low))
      (summation f (+ low 1) high (+ subtotal (f low))))))
```

Last one: Note that it passes along an accumulator.

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## Recursion

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- equally powerful to iteration
- mechanical transformations back and forth
- often more intuitive (sometimes less)
- *naïve* implementation less efficient
  - » no special syntax required
  - » fundamental to functional languages like Scheme

## Expression Evaluation: Short Circuiting

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- Consider `(a < b) && (b < c)`:
  - » If `a >= b` there is no point evaluating whether `b < c` because `(a < b) && (b < c)` is automatically false
- Other similar situations
  - `if (b != 0 && a/b == c) ...`
  - `if (*p && p->foo) ...`
  - `if (f || messy()) ...`